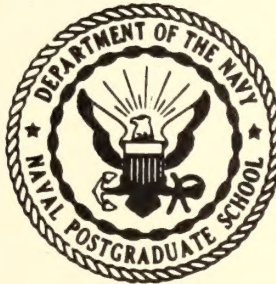


# UNITED STATES NAVAL POSTGRADUATE SCHOOL



## CONFIDENCE INTERVALS FOR THE RELIABILITY CORRECTION FACTOR

by

Paul R. Milch

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ABSTRACT:

As in the Polaris A3 program, whenever extensive test data collected under non-environmental conditions must be used to infer results valid under environmental conditions, the problem of estimation of a correction factor to transform non-environmental results into environmental ones will arise. In the Polaris A3 program, the ratio of mean times under environmental and non-environmental conditions was termed the K-factor. This report presents a solution to the problem of building exact confidence intervals for the K-factor for the case when time is measured in cycles and a specific sampling procedure is feasible.

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## 1. Introduction

The problem of how to utilize extensive test data, accumulated under non-environmental conditions, to infer results on system reliability under environmental conditions arises during the early stages of development of weapons systems. In particular, the problem of estimating the ratio of the mean times to failure under environmental and non-environmental conditions was discussed in a series of reports prepared by the Los Altos office of C-E-I-R, Inc., ([ 5 ], [ 6 ], and [ 7 ]) for the Special Projects Office. This ratio, usually labeled the K-factor, plays the role of a correction factor to transform results obtained under non-environmental conditions to produce new results that would apply under environmental conditions. Since the mean times to failure are unknown quantities under environmental as well as non-environmental conditions, their ratio, the K-factor, is unknown as well. In the reports quoted above, the authors developed estimates of the K-factor for the cases when time to failure is measured continuously as well as in cycles. They also developed confidence interval estimates for the K-factor when time to failure is measured continuously. Apparently exact confidence interval estimates of the K-factor have not been developed for "cycle-type items", i. e., when time to failure is measured in cycles. Although various approximate and asymptotic interval estimates described in the literature



(see [2], [4], and [6]) are adaptable to this problem, no exact confidence interval has been found up to date.

In this report, we develop a confidence interval for the K-factor when cycle-type items are tested. The sampling procedure applied, however, is not sampling to failure (as in [5], [6], and [7]), but is instead sampling to a fixed number of successes.

The confidence interval obtained is one based on the exact (conditional) distribution of the observable random variables. The confidence interval itself may not be called exact only by virtue of the fact that the observable random variables are discrete (see page 513 of [3]), but it should be distinguished from confidence intervals based on approximate distributions of the observable random variables. For this reason, the procedure described in this report is applicable even when only a small number of tests may be performed.





## 2. An Exact Confidence Interval for the K-Factor

We shall assume that a given number of cycle-type items are available for testing under environmental and also under non-environmental conditions. We shall not assume to have the same number of items available for testing under both conditions. In fact, in usual circumstances the number of items available for testing is much larger under non-environmental conditions, for obvious reasons. We further presume that items are tested a fixed number of cycles, or until they fail to function. This procedure is repeated with a given number of items under both environmental and non-environmental conditions until a fixed number of successes, i. e., cycles without failure, are achieved. The number of failures under environmental and non-environmental conditions are two (different) random variables that may be observed in the experiments. We introduce the following notation.

Let

$r_1$  = total number of successes (i. e., cycles without failure) of all items tested under non-environmental conditions;

$r_2$  = total number of successes of all items tested under environmental conditions;

$X$  = total number of failures of all items tested under non-environmental conditions when tests run to the  $r_1^{\text{th}}$  success;



$Y$  = total number of failures of all items tested under environmental conditions when tests run to the  $r_2^{\text{th}}$  success.

As the notation suggests,  $r_1$  and  $r_2$  are numbers fixed usually before the start of the experiments, and  $X$  and  $Y$  are random variables observed at the completion of the experiments.

To facilitate building our probabilistic model, we stipulate the following conditions and notations.

1) Failure or success during a given cycle may occur independently of other failures or successes during other cycles of the same or other items. This may restrict the number of cycles an item may be tested. Items whose future function is affected by their failure during a cycle cannot be tested after their first failure. If repair of an item, however, returns it to its original condition, then such an item may be tested a fixed number of cycles regardless of any number of failures during the tests.

2) The probability of failure,  $q_1$ , during a cycle under non-environmental conditions is the same for all cycles of all items. The same is true for the probability of failure,  $q_2$ , during a cycle under environmental conditions. We have then the following definitions:

$q_1$  = probability of failure during a cycle under non-environmental conditions;

$q_2$  = probability of failure during a cycle under environmental conditions;





$p_1 = 1 - q_1$  = probability of success during a cycle under  
non-environmental conditions;

$p_1 = 1 - q_2$  = probability of success during a cycle under  
environmental conditions.

- 3) Success or failure of an item during a cycle under environmental conditions does not affect the success or failure of any item under environmental conditions.

The above conditions imply that  $X$  and  $Y$  are independent random variables with the negative binomial distribution of parameters,  $r_1, q_1$ , and  $r_2, q_2$ , respectively. Therefore,

$$\begin{aligned} P(X = k) &= \binom{r_1 + k - 1}{k} p_1^{r_1} q_1^k \\ P(Y = k) &= \binom{r_2 + k - 1}{k} p_2^{r_2} q_2^k \end{aligned} \tag{1}$$

for  $k = 0, 1, 2, \dots$ .

Next, we obtain the conditional distribution of  $X$ , given the condition  $X + Y = m$ .

$$\begin{aligned} P(X = k \mid X + Y = m) &= \frac{P(X = k, X + Y = m)}{P(X + Y = m)} \\ &= \frac{P(X = k) P(Y = m - k)}{P(X + Y = m)}. \end{aligned}$$

The distribution of the sum  $X + Y$  is computed routinely:



$$\begin{aligned}
P(X + Y = m) &= \sum_{x=0}^m P(X + Y = m \mid X = x) P(X = x) \\
&= \sum_{x=0}^m P(X = x) P(Y = m - x) \\
&= \sum_{x=0}^m \binom{r_1 + x - 1}{x} \binom{r_2 + m - x - 1}{m - x} p_1^{r_1} p_2^{r_2} q_1^x q_2^{m-x}
\end{aligned}$$

Finally, for  $k = 0, 1, \dots, m$

$$P(X = k \mid X + Y = m) = \frac{\binom{r_1 + k - 1}{k} \binom{r_2 + m - k - 1}{m - k} q^k}{S_m(q; r_1, r_2)} \quad (2)$$

where

$$S_m(q; r_1, r_2) = \sum_{x=0}^m \binom{r_1 + x - 1}{x} \binom{r_2 + m - x - 1}{m - x} q^x$$

and

$$q = \frac{q_1}{q_2}$$

It is of special significance that the conditional distribution of  $X$ , given  $X + Y = m$  (represented by formula (2)), does not depend on  $q_1$  and  $q_2$  themselves but merely on their ratio  $q$ . It is well-known that under the above conditions the mean number of cycles to the first failure (or between consecutive failures) is  $\frac{1}{q_1}$  and  $\frac{1}{q_2}$ , respectively, under non-environmental and environmental conditions. Therefore, the ratio  $q = \frac{q_1}{q_2}$  is also the ratio of the mean number





of cycles to failure under environmental conditions and the mean number of cycles to failure under non-environmental conditions, i. e.,  $q$  is what we called the  $K$ -factor in the introduction. Since the (conditional) distribution of  $X$ , given  $X + Y = m$ , depends on  $q$  alone, a confidence interval for  $q$  may be based on this distribution. Indeed, as in [3], we may always find two real numbers  $\bar{q}$  and  $\underline{q}$  such that

$$\sum_{x=0}^k g_m(x; \bar{q}; r_1, r_2) = \frac{\alpha}{2}$$

and (3)

$$\sum_{x=k}^m g_m(x; \underline{q}; r_1, r_2) = \frac{\alpha}{2},$$

where  $g_m(x; q; r_1, r_2)$  is the conditional probability mass function of  $X$ , given  $X + Y = m$  (presented in formula (2)). Then the interval  $(\underline{q}, \bar{q})$  is a  $100(1 - \alpha)\%$  confidence interval for  $q$ . This must be accompanied with the usual remark that when the observed value of  $X = k = 0$  then  $\underline{q} = 0$ , and when  $X = k = m$  (i. e.,  $Y = 0$ ) then  $\bar{q} = \infty$ , by definition.

One-sided confidence intervals are obtained in a similar manner.

If  $\bar{q}$  and  $\underline{q}$  are determined respectively by

$$\sum_{x=0}^k g_m(x; \bar{q}; r_1, r_2) = \alpha$$
(4)

and

$$\sum_{x=k}^m g_m(x; \underline{q}; r_1, r_2) = \alpha,$$
(5)



then  $(\underline{q}, \infty)$  and  $(0, \bar{q})$  are respectively lower and upper one-sided  $100(1 - \alpha)\%$  confidence intervals for  $q$ . The previous remarks concerning cases when  $k = 0$  or  $k = m$  apply here too.

Unfortunately, the (conditional) distribution  $g_m(x; q; r_1, r_2)$  is not related to any well-known distribution in an explicit way (such as, e. g., the relationship between the binomial and F-distributions) to enable us to obtain percentiles of this (conditional) distribution without further computations. For this reason, we developed tables for the (conditional) distribution  $g_m(x; q; r_1, r_2)$ . Some of these are presented in tables I and II in the appendix.





### 3. Numerical Examples

It is to be expected that whenever non-environmental and environmental test data must be compared, the former will be more extensive than the latter, i. e., in most typical problems we shall find that  $r_1 \gg r_2$ . For this reason, the two cases given most attention in our investigation were:

case 1)  $r_1 = 2r_2$  and  $r_2 = 300, 350, 400, 450, 500$ ; and

case 2)  $r_1 = 10r_2$  and  $r_2 = 10, 20, 30, 40, 50$ .

For these two cases, we developed tables for the percentiles of the cumulative (conditional) distribution function

$$G_m(k; q; r_1, r_2) = \sum_{x=0}^k g_m(x; q; r_1, r_2) . \quad (6)$$

The choice of  $m$  was governed by the fact that the number of failures under both environmental and non-environmental conditions (i. e., the values of  $Y$  and  $X$ ) are usually quite small. For this reason, we let  $0 \leq m \leq 12$  for case 1) and  $0 \leq m \leq 10$  for case 2). Tables I and II of the appendix list the percentiles of  $G_m(k; q; r_1, r_2)$  for cases 1) and 2), respectively. Other cases of interest have been considered. Tables for the distribution function (6) have been prepared (but have not been included in this report) for the following additional cases:



case 3)  $r_1 = r_2 = 400, 500, 600, 700, 800, 900, 1000$  and  
 $0 \leq m \leq 10$  ; and

case 4)  $r_1 = r_2 = 1, 2, 3, 4, 5, 6, 7, 8, 9, 10$  and  
 $0 \leq m \leq 20$  .

Next, we present a few examples of confidence intervals for  $q$  .

- 1) Suppose the experimental data results in four failures under non-environmental conditions when tests have been run until the 300<sup>th</sup> success (i.e., a total of 304 cycles), and in three failures under environmental conditions when tests have been run until the 30<sup>th</sup> success (i.e., a total of 33 cycles). Then,  $r_1 = 300$ ,  $r_2 = 30$ ,  $k = 4$ , and  $m = 7$  . Therefore, from Table II, we find that  $(.0325, .6969)$  is a 90% confidence interval for  $q$  .
- 2) Suppose for  $r_1 = 800$ ,  $r_2 = 400$ , we observed  $X = 4$  and  $Y = 6$  . Then, we have  $k = 4$  and  $m = 10$  . From Table I, we find that  $(.0895, 1.151)$  is a 90% confidence interval for  $q$  .
- 3) For  $r_1 = 800$ ,  $r_2 = 400$ , we observed  $X = 1$  and  $Y = 5$  . Then,  $k = 1$  and  $m = 6$  . From Table I, we find that  $(.0004, 1.474)$  is a two-sided 99% confidence interval for  $q$  .  
 We also find from the same data that  $(0, .5241)$  is a one-sided 90% upper confidence interval for  $q$  .
- 4) For  $r_1 = 1000$ ,  $r_2 = 500$ , we observed  $X = 2$  and  $Y = 5$  . Then,  $k = 2$  and  $m = 7$  . From Table I, we find that  $(.1029, .7409)$  is an 80% confidence interval for  $q$  .



It may be observed that, in general, the confidence intervals for  $q$  were shorter when  $k < m - k$  as compared to when  $k > m - k$ . Indeed, failures during non-environmental tests are usually less frequent than during environmental tests, which indicates that  $q_1 < q_2$  or  $q < 1$ . This fact, of course, is born out by the preceding examples of confidence intervals for  $q$ .





## APPENDIX

TABLE I

PERCENTILES OF THE DISTRIBUTION FUNCTION

$$G_m(k; r_1, r_2)$$



TABLE I  
PERCENTILES OF THE DISTRIBUTION FUNCTION  
 $r_1 = 600, r_2 = 300$   
 $G_m(k; r_1, r_2)$

K/G	.001000 .750000	.005000 .850000	.010000 .900000	.050000 .950000	.100000 .990000	.150000 .995000	.250000 .999000	.500000
0	499.500000 .166675	99.500000 .088234	49.500000 .055556	9.500000 .026315	4.500000 .005050	2.833252 .002513	1.500024 .000500	.500000
0	15.325439 .077581	6.577637 .042458	4.504883 .027131	1.738477 .013031	1.082874 .002527	.792432 .001259	.501031 .000251	.207654
1	997.562500 .4999786	198.921875 .316016	99.085938 .231244	19.216064 .144031	9.229248 .055586	5.897949 .038070	3.227783 .016342	1.205969
0	4.509766 .050635	2.430176 .028013	1.825806 .017990	.860205 .008678	.575523 .001689	.442932 .000842	.295117 .000168	.130695
1	26.697266 .242841	11.570068 .162189	7.984131 .121119	3.193604 .078543	2.053955 .031417	1.546411 .021680	1.032886 .009395	.500818
2	1494.000000 .849951	298.015625 .566278	148.500000 .432831	28.900391 .291608	12.944336 .137378	8.954590 .103229	4.953857 .055621	1.919250
0	2.320557 .037639	1.386511 .020932	1.086414 .013477	.560724 .006517	.391760 .001270	.305609 .000633	.208722 .000126	.095438
1	7.311279 .161426	4.012451 .109773	3.052734 .083664	1.514001 .054450	1.062793 .022077	.841132 .015281	.597742 .006647	.315405
2	37.802734 .420319	16.443604 .298688	11.380371 .236401	4.614258 .165942	3.002930 .082306	2.284668 .067615	1.556360 .034366	.796552
3	1988.750000 .1203711	396.765025 .822150	197.765625 .641345	38.552734 .448059	18.644043 .231274	12.001465 .181201	6.675293 .108264	2.632568



TABLE I  
PERCENTILES OF THE DISTRIBUTION FUNCTION  
 $r_1 = 600, r_2 = 300$   
 $G_m(k, r_1, r_2)$

K/G	$r_1 = 600, r_2 = 300$				$r_1 = 600, r_2 = 300$				$r_1 = 600, r_2 = 300$			
	.001000	.005000	.010000	.050000	.050000	.100000	.150000	.250000	.500000			
	.750000	.850000	.900000	.950000	.950000	.990000	.995000	.999000				
<b>m=5</b>												
0	1.499231	.945057	.761456	.413879	.295270	.233075	.161487	.075243				
	.029989	.016735	.010788	.005224	.001019	.000508	.000101					
1	3.605225	2.207031	1.756848	.963531	.705090	.571619	.418671	.230420				
	.121234	.083435	.063824	.041798	.017070	.011833	.005157					
2	10.002930	5.531982	4.230469	2.142334	1.528467	1.226111	.892767	.501672				
	.281873	.205243	.164661	.117480	.059489	.045491	.025159					
3	48.798828	21.267578	14.742432	6.020508	3.942871	3.016113	2.075928	1.092212				
	.601123	.440277	.356909	.261182	.143237	.114032	.069805					
4	2482.000000	495.203125	246.859375	48.173828	23.328125	15.038818	8.391357	3.344482				
	1.558313	1.079761	.852332	.608020	.330511	.265149	.167865					
<b>m=6</b>												
0	1.089893	.715710	.582941	.327582	.236859	.188402	.131793	.062168				
	.024953	.013954	.009002	.004364	.000852	.000425	.000085					
1	2.265381	1.475610	1.205237	.700391	.525110	.431763	.321936	.181720				
	.097227	.067337	.051684	.033980	.013938	.009672	.004221					
2	4.823242	2.984863	2.392090	1.346106	1.003955	.826482	.621997	.366492				
	.212842	.157001	.126849	.091310	.046777	.035876	.019924					
3	12.650879	7.026367	5.388916	2.760742	1.987061	1.605664	1.184436	.687823				
	.405273	.304959	.251080	.187274	.105365	.084453	.052260					
4	59.724609	26.062500	18.083008	7.418213	4.877197	3.743408	2.592529	1.387244				
	.783002	.583856	.480042	.359900	.209149	.170825	.111285					
5	2973.500000	593.312500	295.781250	57.761719	27.958047	18.066162	10.102051	4.054688				
	1.912659	1.337927	1.064197	.769513	.432404	.352175	.231274					









TABLE I  
PERCENTILES OF THE DISTRIBUTION FUNCTION  
 $r_1 = 600, r_2 = 300$

K/G	.001000 .005000 .750000	.010000 .050000 .900000	.050000 .950000	.100000 .900000	.150000 .950000	.250000 .999000	.500000



TABLE I  
PERCENTILES OF THE DISTRIBUTION FUNCTION  
 $r_1 = 600, r_2 = 300$   
 $G_m(k, r_1, r_2)$

K/G	.001000 .750000	.005000 .850000	.010000 .900000	.050000 .950000	.100000 .990000	.150000 .995000	.250000 .999000	.500000
m=10								
0	.506921 .015022	.356543 .008436	.298749 .005453	.178851 .002648	.132739 .000518	.107166 .000258	.076361 .000052	.036910
1	.839880 .054694	.606219 .038318	.516931 .029592	.331235 .019596	.259015 .008106	.218243 .005634	.167926 .002464	.099149
2	1.287085 .108722	.930756 .081854	.796582 .066964	.520929 .048901	.414490 .025533	.354559 .019680	.280377 .011009	.177722
3	1.952148 .179370	1.395789 .139880	1.190562 .117542	.777814 .085935	.621535 .052443	.534357 .042435	.427094 .026666	.279279
4	3.040283 .273297	2.122559 .216962	1.794263 .184555	1.152148 .145160	.916504 .090005	.786908 .074854	.629474 .050223	.415924
5	5.052002 .403076	3.389648 .322424	2.819052 .276837	1.747754 .220227	1.371802 .141406	1.169543 .119525	.928436 .083454	.610034
6	9.514648 .594080	5.978760 .474823	4.837891 .408234	2.821045 .326208	2.158691 .213116	1.813965 .181781	1.414514 .129962	.908508
7	23.046875 .904907	12.893066 .715619	9.536275 .612170	5.188232 .487061	3.789063 .318518	3.098145 .272595	2.333740 .197131	1.427759
8	102.953125 1.510828	45.029257 1.162463	31.298828 .579584	12.946777 .765759	8.572598 .490814	6.621094 .418549	4.638672 .302100	2.558838
9	4923.375000 3.322510	582.500000 2.367188	489.506250 1.511316	95.802734 1.418542	46.519531 .849219	30.076172 .711621	16.889160 .500513	6.873779





TABLE 1

PERCENTILES OF THE DISTRIBUTION FUNCTION

 $G_m(k, r_1, r_2)$  $r_1 = 600, r_2 = 300$ 

K/G

K/G	$m = 11$									
	$r_1 = 600, r_2 = 300$	$r_1 = 600, r_2 = 300$	$r_1 = 600, r_2 = 300$	$r_1 = 600, r_2 = 300$	$r_1 = 600, r_2 = 300$	$r_1 = 600, r_2 = 300$	$r_1 = 600, r_2 = 300$	$r_1 = 600, r_2 = 300$	$r_1 = 600, r_2 = 300$	$r_1 = 600, r_2 = 300$
0	.001000 .750000	.005000 .850000	.010000 .900000	.050000 .950000	.100000 .990000	.150000 .995000	.250000 .999000	.500000 .	.500000 .	.500000 .
1	.446320 .013683	.316687 .007688	.266370 .004971	.160785 .002415	.119739 .000472	.096876 .	.069191 .000047	.033553 .	.033553 .	.033553 .
2	.720959 .049386	.526727 .034648	.451477 .026780	.292798 .017749	.230054 .007351	.194446 .005110	.150195 .002235	.049180 .	.049180 .	.049180 .
3	1.071033 .097066	.787213 .073258	.678394 .060017	.450836 .043508	.361273 .022977	.310339 .017719	.246777 .009920	.157703 .	.157703 .	.157703 .
4	1.559351 .157855	1.139626 .123553	.981354 .104053	.655292 .079832	.528741 .046731	.457245 .037852	.368292 .023824	.243665 .	.243665 .	.243665 .
5	2.293457 .236005	1.650769 .188342	1.413721 .161090	.935852 .126941	.754529 .079168	.653156 .065949	.528101 .044370	.354712 .	.354712 .	.354712 .
6	2.498535 .339117	2.453125 .273389	2.079102 .235822	1.346777 .188708	1.077686 .122241	.929596 .103595	.749402 .072641	.504114 .	.504114 .	.504114 .
7	5.727539 .481232	3.853516 .389105	3.209961 .336829	2.001953 .271558	1.577661 .179767	1.349341 .153949	1.076892 .110797	.716473 .	.716473 .	.716473 .
8	10.666260 .690051	6.714623 .558811	5.438222 .480652	3.183350 .387823	2.442627 .256984	2.056985 .223004	1.609814 .162982	1.043018 .	1.043018 .	1.043018 .
9	25.615234 .1029773	14.341757 .818824	11.059326 .703473	5.787598 .563684	4.234131 .374609	3.467041 .322821	2.618164 .237286	1.611340 .	1.611340 .	1.611340 .
10	113.656250 .1691968	49.726563 .1306921	34.572266 .1104602	14.315918 .867526	9.488525 .562921	7.333984 .482483	5.145752 .352484	2.849609 .	2.849609 .	2.849609 .
11	5406.875000 .3.672363	1079.000000 .2.623047	538.062500 .2.122070	105.234375 .1.580469	51.113281 .954041	33.054688 .802405	18.572021 .569391	7.572998 .	7.572998 .	7.572998 .



TABLE I  
PERCENTILES OF THE DISTRIBUTION FUNCTION

K/G

 $r_1 = 600, r_2 = 300$  $m=12$ 

K/G	.001000 .750000	.005000 .850000	.010000 .500000	.050000 .950000	.100000 .900000	.150000 .995000	.250000 .999000	.500000
C	.398657 .012549	.284955 .007065	.240355 .004570	.146106 .002220	.109119 .000434	-.088428 -.000216	.064290 .000043	.030776
1	.631091 .045041	.465607 .031638	.400726 .024473	.262402 .016231	.207013 .006727	.175403 .004678	.135913 .002047	.081077
2	.915253 .087740	.681384 .066384	.590417 .054415	.397437 .039863	.320258 .020902	.276044 .016124	.220502 .009035	.141864
3	1.292450 .141071	.960663 .110736	.833228 .093412	.565912 .071829	.460083 .042172	.399655 .034190	.323859 .021547	.216229
4	1.825256 .207847	1.343726 .166524	1.161914 .142810	.786847 .112903	.640867 .070734	.558191 .059001	.455017 .039783	.305454
5	2.625883 .293073	1.902222 .237622	1.623618 .205670	1.091785 .165332	.885931 .107806	.770642 .091535	.628223 .064400	.429932
6	3.952637 .405212	2.780762 .330328	2.361084 .287335	1.539697 .233126	1.227585 .155911	1.071216 .133807	.868236 .096788	.522065
7	6.398442 .559442	4.314209 .450055	3.598389 .357192	2.454639 .323523	1.782300 .219067	1.528101 .189441	1.224585 .135453	.822577
8	11.812012 .705992	7.444824 .636890	6.035645 .553278	3.543701 .449799	2.724854 .305487	2.298584 .264366	1.804321 .190348	1.177173
9	28.171875 .1154346	15.784668 .922089	12.177734 .794812	6.384766 .640491	4.677490 .431122	3.834229 .373572	2.901367 .278119	1.744324
10	124.328125 .1872620	54.408203 .1451074	37.823984 .1229468	15.680176 .970062	10.400635 .835213	8.044185 .646716	5.650879 .403351	3.139160
11	548.750000 .4021424	1175.250000 .2878174	586.000000 .232275	114.640625 .1742017	55.68453 .1058765	36.021484 .993225	20.250000 .38477	8.269775



TABLE I

## PERCENTILES OF THE DISTRIBUTION FUNCTION

 $r_1 = 700 \quad r_2 = 350$  $G_m(k; r_1, r_2)$ 

K/G	m=1					m=2					m=3					m=4					m=5					
0	455.500000 .166675	59.500000 .088234	6.576660 .042430	44.500000 .055556	9.500000 .026315	4.500000 .005050	1.738110 .013027	1.082625 .002526	2.833252 .002513	1.500024 .000500	59.500000 .088234	6.576660 .042430	44.500000 .055556	9.500000 .026315	4.500000 .005050	1.738110 .013027	1.082625 .002526	2.833252 .002513	1.500024 .000500	59.500000 .088234	6.576660 .042430	44.500000 .055556	9.500000 .026315	4.500000 .005050	1.738110 .013027	1.082625 .002526
C	15.323242 .077547																									
1	997.812500 .499817	158.968750 .316016	59.109375 .231244	59.109375 .231244	15.220459 .144031	9.231201 .055583	5.899170 .038066	3.228271 .016338	5.899170 .038066	3.228271 .016338	158.968750 .316016	59.109375 .231244	59.109375 .231244	15.220459 .144031	9.231201 .055583	5.899170 .038066	3.228271 .016338	5.899170 .038066	3.228271 .016338	158.968750 .316016	59.109375 .231244	59.109375 .231244	15.220459 .144031	9.231201 .055583	5.899170 .038066	3.228271 .016338
0	4.508301 .050589	2.429159 .027986	6.576660 .042430	1.825073 .017971	8.59778 .008671	5.75187 .001688	4.42657 .000941	2.94904 .000168	4.42657 .000941	2.94904 .000168	2.429159 .027986	6.576660 .042430	1.825073 .017971	8.59778 .008671	5.75187 .001688	4.42657 .000941	2.94904 .000168	4.42657 .000941	2.94904 .000168	2.429159 .027986	6.576660 .042430	1.825073 .017971	8.59778 .008671	5.75187 .001688	4.42657 .000941	2.94904 .000168
1	26.701172 .242749	11.571045 .162128	7.984863 .122058	7.984863 .122058	3.193604 .078505	2.053955 .031398	1.546289 .021669	1.032764 .009390	1.546289 .021669	1.032764 .009390	11.571045 .162128	7.984863 .122058	7.984863 .122058	3.193604 .078505	2.053955 .031398	1.546289 .021669	1.032764 .009390	1.546289 .021669	1.032764 .009390	11.571045 .162128	7.984863 .122058	7.984863 .122058	3.193604 .078505	2.053955 .031398	1.546289 .021669	1.032764 .009390
2	1494.750000 .850134	298.156250 .566370	148.578125 .432861	148.578125 .432861	28.914063 .291608	13.950435 .137378	8.958496 .103198	4.955811 .055609	8.958496 .103198	4.955811 .055609	298.156250 .566370	148.578125 .432861	148.578125 .432861	28.914063 .291608	13.950435 .137378	8.958496 .103198	4.955811 .055609	4.955811 .055609	2.94904 -.000168	298.156250 .566370	148.578125 .432861	148.578125 .432861	28.914063 .291608	13.950435 .137378	8.958496 .103198	4.955811 .055609
C	2.319336 .037589	1.385556 .020906																								
1	7.310791 .161304	4.011963 .109882	3.052246 .083587	3.052246 .083587	1.513635 .054400	1.062427 .022054	.840796 .015262	.597467 .006639	.305304 .000632	.208478 -.000126	4.011963 .109882	3.052246 .083587	3.052246 .083587	1.513635 .054400	1.062427 .022054	.840796 .015262	.597467 .006639	.305304 .000632	.208478 -.000126	4.011963 .109882	3.052246 .083587	3.052246 .083587	1.513635 .054400	1.062427 .022054	.840796 .015262	.597467 .006639
2	37.802027 .420226	16.448730 .298556	11.203789 .236310	11.203789 .236310	4.615477 .165881	3.003662 .082220	2.285156 .062580	1.556543 .034343	2.285156 .062580	1.556543 .034343	16.448730 .298556	11.203789 .236310	11.203789 .236310	4.615477 .165881	3.003662 .082220	2.285156 .062580	1.556543 .034343	1.556543 .034343	6.679443 .108264	16.448730 .298556	11.203789 .236310	11.203789 .236310	4.615477 .165881	3.003662 .082220	2.285156 .062580	1.556543 .034343
3	1990.250000 .1204199	397.046875 .822394	157.506250 .641498	157.506250 .641498	38.580078 .448120	18.656738 .231274	12.009521 .181201	6.679443 .108264	12.009521 .181201	6.679443 .108264	397.046875 .822394	157.506250 .641498	157.506250 .641498	38.580078 .448120	18.656738 .231274	12.009521 .181201	6.679443 .108264	6.679443 .108264	2.634033	1990.250000 .1204199	397.046875 .822394	157.506250 .641498	157.506250 .641498	38.580078 .448120	12.009521 .181201	6.679443 .108264
0	1.497949 .029545	.948181 .016704	.760663 .010768	.760663 .010768	.413391 .005214	.254873 .001017	.232739 .000507	.161243 .000101	.232739 .000507	.161243 .000101	.948181 .016704	.760663 .010768	.760663 .010768	.413391 .005214	.254873 .001017	.232739 .000507	.161243 .000101	.161243 .000101	.075117	1.497949 .029545	.948181 .016704	.760663 .010768	.760663 .010768	.413391 .005214	.232739 .000507	.161243 .000101
1	3.604248 .121082	2.206294 .083324	1.756055 .063736	1.756055 .063736	.962952 .041741	.704602 .017044	.571161 .011814	.418304 .005150	.571161 .011814	.418304 .005150	2.206294 .083324	1.756055 .063736	1.756055 .063736	.962952 .041741	.704602 .017044	.571161 .011814	.418304 .005150	.418304 .005150	.230176	3.604248 .121082	2.206294 .083324	1.756055 .063736	1.756055 .063736	.962952 .041741	.704602 .017044	.571161 .011814
2	10.004639 .281689	5.532471 .205090	4.230957 .164508	4.230957 .164508	2.142334 .117358	1.528284 .059428	1.225928 .045445	.892523 .025132	1.225928 .045445	.892523 .025132	5.532471 .205090	4.230957 .164508	4.230957 .164508	2.142334 .117358	1.528284 .059428	1.225928 .045445	.892523 .025132	.892523 .025132	.501428	10.004639 .281689	5.532471 .205090	4.230957 .164508	4.230957 .164508	2.142334 .117358	1.528284 .059428	.892523 .025132
3	48.826172 .601062	21.279257 .440186	14.750488 .356848	14.750488 .356848	6.023438 .261090	3.944580 .143176	3.017334 .113971	2.067616 .069760	3.017334 .113971	2.067616 .069760	21.279257 .440186	14.750488 .356848	14.750488 .356848	6.023438 .261090	3.944580 .143176	3.017334 .113971	2.067616 .069760	2.067616 .069760	1.092334	48.826172 .601062	21.279257 .440186	14.750488 .356848	14.750488 .356848	6.023438 .261090	3.944580 .143176	2.067616 .069760
4	2484.250000 .1559229	455.671875 .1080310	247.093750 .852658	247.093750 .852658	48.218750 .608203	23.349609 .2330542	15.052246 .265179	8.398682 .167834	15.052246 .265179	8.398682 .167834	455.671875 .1080310	247.093750 .852658	247.093750 .852658	48.218750 .608203	23.349609 .2330542	15.052246 .265179	8.398682 .167834	8.398682 .167834	3.347168	2484.250000 .1559229	455.671875 .1080310	247.093750 .852658	247.093750 .852658	48.218750 .608203	23.349609 .2330542	15.052246 .265179



















TABLE 1

PERCENTILES OF THE DISTRIBUTION FUNCTION  $G_m(k, r_1, r_2)$ 

K/G	$r_1 = 700$		$r_2 = 350$		$G_m(k, r_1, r_2)$	
	$r_1 = 700$	$r_2 = 350$	$r_1 = 700$	$r_2 = 350$	$G_m(k, r_1, r_2)$	$G_m(k, r_1, r_2)$
0	.001000 .750000	.005000 .850000	.010000 .900000	.050000 .950000	.150000 .995000	.250000 .999000
1	.44977 .013622	.31563 .07652	.265454 .004949	.160175 .002403	.096482 -.000235	.068901 .000047
2	.719373 .049187	.525415 .034507	.450287 .026670	.291913 .017677	.193305 .005089	.149677 .002227
3	1.069365 .096738	.785779 .073042	.677081 .059805	.449799 .043748	.309546 .017650	.246106 .009882
4	1.557825 .157428	1.138293 .123187	.980072 .103748	.654224 .075584	.456360 .037726	.367499 .023744
5	2.292480 .235886	1.649854 .187915	1.412744 .160693	.934906 .126636	.652301 .065162	.527338 .044240
6	3.499023 .338679	2.453125 .272931	2.078857 .235354	1.346284 .188342	.929016 .103351	.748792 .072462
7	5.731201 .480815	3.855469 .388708	3.211426 .336432	2.002441 .271191	1.349341 .153674	1.076709 .110583
8	10.678223 .689929	6.720703 .555597	5.443604 .480408	3.185791 .387549	2.058105 .222760	1.610547 .162769
9	25.656250 .1030261	14.363770 .819128	11.075684 .703595	5.795654 .563664	3.471191 .322668	2.620850 .237103
10	112.875000 .1.693982	49.824219 .1.308264	34.638672 .1.105640	14.342773 .868536	7.346924 .482574	5.154297 .352454
11	5419.625000 .3.679443	1081.500000 .2.627686	539.312500 .2.175732	105.484375 .1.582849	33.130859 .803158	18.614014 .569788
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TABLE 1

PERCENTILES OF THE DISTRIBUTION FUNCTION  $G_m(k; r_1, r_2)$ 

K/G	$r_1 = 800 \quad r_2 = 400$				$G_m(k; r_1, r_2)$			
	.005000	.010000	.020000	.050000	.150000	.250000	.500000	
	.001000	.010000	.020000	.050000	.150000	.250000	.500000	
	.750000	.900000	.950000	.990000	.995000	.999000		
<b>m=5</b>								
1	1.497034	.947473	.760063	.412994	.294558	.232465	.161060	.075022
	.029897	.016681	.010753	.005207	.001017	.000506	.000101	
2	3.603516	2.205611	1.755502	.962524	.704236	.570825	.417999	.229993
	.120959	.043240	.063671	.041695	.017025	.011902	.005144	
3	10.005559	5.532959	4.231201	2.142334	1.528162	1.225745	.892340	.501245
	.261567	.204964	.164417	.117267	.059382	.045407	.025110	
4	48.847656	21.259063	14.756348	6.025635	3.946045	3.018311	2.076904	1.092456
	.601062	.440159	.356757	.261029	.143115	.113910	.069725	
5	2486.125000	496.015625	247.265622	48.251953	23.365234	15.062500	8.404053	3.349121
	1.559961	1.080737	.852972	.608356	.330542	.265179	.167834	
<b>m=6</b>								
1	1.087695	.714093	.581506	.326636	.236127	.187793	.131335	.061932
	.024854	.013896	.008966	.004346	.000849	.000423	.000084	
2	2.263184	1.473840	1.203650	.699207	.524103	.430847	.321204	.181232
	.096937	.067124	.051520	.03870	.013893	.009638	.004206	
3	4.622998	2.944131	2.391357	1.345251	1.003101	.825690	.621265	.365912
	.212415	.126665	.126575	.091093	.046655	.035781	.019870	
4	12.659912	7.030762	5.391346	2.761719	1.987488	1.605786	1.184314	.694888
	.404907	.304663	.250775	.187000	.105182	.084297	.052157	
5	59.803594	26.095009	18.107910	7.427490	4.882813	3.747559	2.594971	1.388098
	.783215	.543856	.479980	.359778	.208997	.170673	.111163	
6	2979.625000	594.562500	296.406250	57.880859	28.052734	18.102051	10.121338	4.061768
	1.915405	1.339214	1.065356	.770184	.432587	.352271	.231274	





TABLE 1  
PERCENTILES OF THE DISTRIBUTION FUNCTION  $G_m(k, r_1, r_2)$   
 $r_1 = 800$   $r_2 = 400$

K · G	0.01000	.005000	.010000	.020000	.050000	.100000	.150000	.250000	.500000
0	.847998 .021283	.570917 .011917	.469786 .007696	.270032 .003733	.197040 .000729	.157550 .000363	.110919 .000073	.052771	
1	1.612683 .080955	1.092700 .026300	.907288 .043309	.547113 .028547	.416656 .011745	.345709 .008154	.260785 .003561	.149646	
2	2.982422 .170625	1.957634 .127032	1.620007 .103107	.968842 .074614	.741496 .036497	.619800 .029560	.475677 .016471	.288342	
3	6.016602 .306525	3.745650 .234052	3.013672 .194293	1.720166 .146411	1.296301 .083576	1.076099 .067238	.821722 .041863	.501855	
4	15.290527 .529504	8.515137 .406372	6.542480 .339667	3.375486 .259961	2.442871 .155475	1.982910 .127979	1.474390 .084450	.873480	
5	70.726563 .965790	30.888672 .728528	21.445313 .604480	8.823242 .460358	5.815674 .277600	4.473877 .230511	3.111328 .156177	1.683179	
6	3472.000000 2.270508	692.812200 1.598474	345.406250 1.278174	67.484375 .932770	32.730469 .536127	21.134766 .441162	11.834473 .297009	4.772949	



TABLE I  
PERCENTILES OF THE DISTRIBUTION FUNCTION  $G_m(k; r_1, r_2)$   
 $r_1 = 800$   $r_2 = 400$

$K \cdot G$	.005000	.010000	.050000	.100000	.150000	.250000	.500000
	.850000	.900000	.950000	.990000	.995000	.999000	
0	.847998 .021283	.570917 .011917	.469788 .007696	.270032 .003733	.197040 .000729	.157550 .000363	.110919 .000073
1	1.612663 .080955	1.022700 .056500	.907288 .043309	.547113 .028547	.416656 .011745	.345709 .008154	.260785 .003561
2	2.942422 .170625	1.957834 .127032	1.620007 .103107	.968842 .074614	.741498 .038497	.619800 .029580	.475677 .016471
3	6.016602 .306525	3.745850 .234052	3.013672 .194293	1.720166 .146411	1.296301 .083576	1.076099 .067238	.821722 .041863
4	15.290527 .529504	8.515137 .406372	6.542480 .339667	3.375488 .259961	2.442871 .155475	1.982910 .127979	1.474390 .084450
5	70.726563 .965790	30.888672 .728528	21.445313 .604480	8.823242 .460358	5.815674 .277600	4.473877 .230511	3.111328 .156177
6	3472.000000 2.270508	692.812500 1.598474	345.406250 1.278174	67.484375 .932770	32.730469 .536127	21.134766 .441162	11.834473 .297009



TABLE I  
PERCENTILES OF THE DISTRIBUTION FUNCTION

[illegible]



TABLE I  
PERCENTILES OF THE DISTRIBUTION FUNCTION  $G_m(k, r_1, r_2)$

K/G	$r_1 = 800 \quad r_2 = 400$		$r_1 = 1000 \quad r_2 = 500$		$r_1 = 1500 \quad r_2 = 750$		$r_1 = 2000 \quad r_2 = 1000$		$r_1 = 3000 \quad r_2 = 1500$		$r_1 = 4000 \quad r_2 = 2000$		$r_1 = 5000 \quad r_2 = 2500$		$r_1 = 6000 \quad r_2 = 3000$		$r_1 = 7000 \quad r_2 = 3500$		$r_1 = 8000 \quad r_2 = 4000$		$r_1 = 9000 \quad r_2 = 4500$		$r_1 = 10000 \quad r_2 = 5000$	
	$r_1 = 800$	$r_2 = 400$	$r_1 = 1000$	$r_2 = 500$	$r_1 = 1500$	$r_2 = 750$	$r_1 = 2000$	$r_2 = 1000$	$r_1 = 3000$	$r_2 = 1500$	$r_1 = 4000$	$r_2 = 2000$	$r_1 = 5000$	$r_2 = 2500$	$r_1 = 6000$	$r_2 = 3000$	$r_1 = 7000$	$r_2 = 3500$	$r_1 = 8000$	$r_2 = 4000$	$r_1 = 9000$	$r_2 = 4500$	$r_1 = 10000$	$r_2 = 5000$
m=9																								
0	.584100 .016559	.406158 .009290	.338721 .006004	.200574 .002914	.148181 .000570	.119342 .000284	.084751 .000057	.040784																
1	1.001066 .061001	.711285 .042653	.602496 .032908	.380225 .021764	.295239 .008989	.247815 .006246	.189685 .002731	.111163																
2	1.601025 .123126	1.133105 .092439	.960876 .075441	.615070 .054968	.484802 .028611	.412384 .022031	.323706 .012310	.202893																
3	2.574707 .207257	1.786389 .160815	1.504419 .134723	.953796 .102710	.752179 .059573	.641528 .048138	.507440 .030177	.326575																
4	4.372803 .324438	2.922363 .255627	2.424805 .216992	1.490991 .169330	1.163623 .104144	.987701 .086399	.778241 .057742	.502496																
5	8.366455 .497589	5.245117 .393561	4.238281 .335669	2.458496 .264722	1.874207 .167834	1.570215 .141345	1.218298 .098066	.773145																
6	20.509766 .779980	11.459229 .612292	8.824463 .520807	4.593262 .410492	3.346680 .262769	2.731445 .222821	2.050781 .157703	1.244360																
7	92.451172 1.331091	40.421875 1.018909	28.087891 .855139	11.601318 .664020	7.672607 .419067	5.919434 .354987	4.138916 .252209	2.271484																
8	4453.000000 2.979004	888.625000 2.115723	443.079125 1.703748	86.623047 1.258765	42.048828 .745435	27.175781 .621661	15.248291 .432281	6.190430																









TABLE I  
PERCENTILES OF THE DISTRIBUTION FUNCTION  
 $r_1 = 800$   $r_2 = 400$   
 $G_m(k; r_1, r_2)$

K/G	$r_1 = 800$		$r_2 = 400$		$G_m(k; r_1, r_2)$	
	.001000 .750000	.005000 .850000	.010000 .900000	.050000 .950000	.100000 .990000	.150000 .995000
0	.001000 .750000	.005000 .850000	.010000 .900000	.050000 .950000	.100000 .990000	.150000 .995000
1	.001000 .750000	.005000 .850000	.010000 .900000	.050000 .950000	.100000 .990000	.150000 .995000
2	.001000 .750000	.005000 .850000	.010000 .900000	.050000 .950000	.100000 .990000	.150000 .995000
3	.001000 .750000	.005000 .850000	.010000 .900000	.050000 .950000	.100000 .990000	.150000 .995000
4	.001000 .750000	.005000 .850000	.010000 .900000	.050000 .950000	.100000 .990000	.150000 .995000
5	.001000 .750000	.005000 .850000	.010000 .900000	.050000 .950000	.100000 .990000	.150000 .995000
6	.001000 .750000	.005000 .850000	.010000 .900000	.050000 .950000	.100000 .990000	.150000 .995000
7	.001000 .750000	.005000 .850000	.010000 .900000	.050000 .950000	.100000 .990000	.150000 .995000
8	.001000 .750000	.005000 .850000	.010000 .900000	.050000 .950000	.100000 .990000	.150000 .995000
9	.001000 .750000	.005000 .850000	.010000 .900000	.050000 .950000	.100000 .990000	.150000 .995000
10	.001000 .750000	.005000 .850000	.010000 .900000	.050000 .950000	.100000 .990000	.150000 .995000



TABLE I  
PERCENTILES OF THE DISTRIBUTION FUNCTION  $G_m(k; r_1, r_2)$   
 $r_1 = 800$   $r_2 = 400$

$K \cdot G$	$r_1 = 800$	$r_2 = 400$	$m = 12$	$G_m(k; r_1, r_2)$
0	.001000 .750000	.010000 .900000	.050000 .950000	.150000 .995000 .250000 .999000
1	.396307 .012458	.233093 .007004	.145038 .002201	.087730 -.000215 .062775 .000043
2	.628223 .044694	.463226 .031390	.260815 .016101	.174243 .004640 .134998 .002030
3	.912170 .087147	.678760 .065922	.395544 .039577	.274579 .016006 .219250 .008966
4	1.289526 .140277	.920069 .110095	.563898 .071379	.398016 .033961 .322424 .021402
5	1.822998 .206921	1.341224 .165790	.784955 .112323	.639117 .070337 .453491 .039546
6	2.629395 .292065	1.901123 .236737	1.090381 .164630	.884497 .107318 .769238 .064072
7	3.955322 .404266	2.791738 .329443	1.539331 .232404	1.236975 .155231 .867651 .096384
8	6.408447 .558601	4.320068 .455383	2.256348 .322852	1.783337 .218488 1.224707 .139026
9	11.840332 .785992	7.461426 .636676	3.550293 .449402	2.729492 .305029 1.806458 .196521
10	28.261719 1.155811	15.833252 .922913	6.402588 .640674	4.689697 .430969 2.907959 .277814
11	124.812500 1.877258	54.617184 1.454243	15.738281 .971619	10.437988 .635791 5.669922 .403381
12	5915.375000 4.036621	1180.500000 2.888423	115.156250 1.747266	55.939453 1.061267 20.337891 .639453









TABLE 1  
PERCENTILES OF THE DISTRIBUTION FUNCTION  $G_m(k, r_1, r_2)$   
 $r_1 = 900 \quad r_2 = 450$

$k \cdot G$	.010000	.015000	.010000	.050000	.100000	.150000	.250000	.500000
	.830000	.900000	.900000	.950000	.990000	.995000	.999000	
m=5								
1	1.496301	.946960	.759625	.412689	.294324	.232281	.160907	.074946
	.029863	.016662	.010742	.005201	.001015	.000506	.000101	
2	3.602763	2.205322	1.755078	.962189	.703931	.570581	.417786	.229840
	.120866	.033175	.063622	.041661	.017013	.011791	.005138	
3	10.006836	5.533447	4.231445	2.142334	1.528101	1.225623	.892218	.501123
	.281445	.204877	.164325	.117206	.059344	.045380	.025094	
4	48.863281	21.236875	14.761230	6.027344	3.947021	3.019043	2.077393	1.092578
	.601031	.440094	.356726	.260968	.143085	.113879	.069699	
5	2487.500000	496.236875	247.406250	48.279297	23.378906	15.070313	8.408203	3.351586
	1.560510	1.041042	.853156	.606478	.330573	.265179	.167804	
m=6								
1	1.086963	.713544	.581049	.326300	.235883	.187579	.131183	.061856
	.024820	.013877	.008955	.004340	.000847	.000423	.000084	
2	2.262451	1.473291	1.203101	.698810	.523767	.430573	.320959	.181049
	.096841	.067052	.051463	.033832	.013877	.009628	.004201	
3	4.822754	2.943887	2.391113	1.345007	1.002856	.825415	.621021	.365729
	.212262	.156543	.126433	.091016	.046613	.035747	.019851	
4	12.662842	7.032227	5.392822	2.761963	1.987610	1.605847	1.184253	.687396
	.404785	.304541	.250684	.186908	.105121	.084247	.052123	
5	59.837691	26.111328	18.115967	7.430420	4.884521	3.748779	2.595947	1.388403
	.783276	.533856	.479950	.359747	.208936	.170642	.111102	
6	2981.750000	594.937500	296.609375	57.919922	28.072266	18.114014	10.127930	4.063965
	1.916321	1.340063	1.065723	.770398	.432648	.352301	.231274	



TABLE I

PERCENTILES OF THE DISTRIBUTION FUNCTION

 $G_m(k; r_1, r_2)$  $r_1 = 900 \quad r_2 = 450$ 

K/G

	.010000	.015000	.020000	.025000	.030000	.040000	.050000	.060000	.070000	.080000	.090000	.100000	.150000	.250000	.500000
1	.001000	.005000	.010000	.015000	.020000	.030000	.040000	.050000	.060000	.070000	.080000	.090000	.150000	.250000	.500000
2	.001000	.005000	.010000	.015000	.020000	.030000	.040000	.050000	.060000	.070000	.080000	.090000	.150000	.250000	.500000
3	.001000	.005000	.010000	.015000	.020000	.030000	.040000	.050000	.060000	.070000	.080000	.090000	.150000	.250000	.500000
4	.001000	.005000	.010000	.015000	.020000	.030000	.040000	.050000	.060000	.070000	.080000	.090000	.150000	.250000	.500000
5	.001000	.005000	.010000	.015000	.020000	.030000	.040000	.050000	.060000	.070000	.080000	.090000	.150000	.250000	.500000
6	.001000	.005000	.010000	.015000	.020000	.030000	.040000	.050000	.060000	.070000	.080000	.090000	.150000	.250000	.500000
7	.001000	.005000	.010000	.015000	.020000	.030000	.040000	.050000	.060000	.070000	.080000	.090000	.150000	.250000	.500000
8	.001000	.005000	.010000	.015000	.020000	.030000	.040000	.050000	.060000	.070000	.080000	.090000	.150000	.250000	.500000
9	.001000	.005000	.010000	.015000	.020000	.030000	.040000	.050000	.060000	.070000	.080000	.090000	.150000	.250000	.500000
10	.001000	.005000	.010000	.015000	.020000	.030000	.040000	.050000	.060000	.070000	.080000	.090000	.150000	.250000	.500000

m=7





TABLE I

PERCENTILES OF THE DISTRIBUTION FUNCTION

 $G_m(k; r_1, r_2)$  $r_1 = 900 \quad r_2 = 450$  $k/G$ 

0	.001000	.005000	.010000	.020000	.100000	.150000	.250000	.500000
	.750000	.850000	.900000	.950000	.990000	.995000	.999000	
1	1.238623	.862463	.724347	.448334	.345221	.288312	.219281	.127338
	.069443	.042440	.037322	.024648	.010162	.007059	.003045	
2	2.100566	1.444360	1.209875	.752911	.586206	.494995	.384894	.237636
	.142871	.106830	.086971	.063183	.032764	.025205	.014064	
3	3.682617	2.442485	2.025146	1.231421	.953613	.804510	.627368	.395239
	.246699	.190295	.158832	.120502	.069424	.055995	.035003	
4	7.197998	4.499512	3.628906	2.090820	1.586267	1.323950	1.020435	.637469
	.401561	.313147	.264203	.204602	.124408	.102893	.068413	
5	17.915039	9.995605	7.689697	3.987305	2.896729	2.358643	1.763501	1.059253
	.654590	.508966	.429779	.334601	.208234	.174426	.119952	
6	81.666016	35.639453	24.789063	10.221436	6.750000	5.200928	3.627930	1.978516
	1.148853	.873846	.729779	.561945	.347815	.292096	.203412	
7	3966.875000	791.625000	394.687500	77.138672	37.429688	24.181641	13.555968	5.487061
	2.627197	1.858459	1.491907	1.096301	.640735	.531244	.364233	

 $m = 8$























TABLE I  
PERCENTILES OF THE DISTRIBUTION FUNCTION  $G_m(k; r_1, r_2)$

K, G	$r_1 = 1000$		$r_2 = 500$		$G_m(k; r_1, r_2)$
	$r_1 = 1000$	$r_2 = 500$	$r_1 = 1000$	$r_2 = 500$	
1	.001000	.010000	.050000	.150000	.250000
	.750000	.900000	.950000	.995000	.999000
					.500000
m=1					
1	499.500000	99.500000	9.500000	4.500000	2.833252
	.166675	.048234	.026315	.005050	.002513
					.500000
m=2					
1	15.319824	6.574951	1.737500	1.082202	.791852
	.077490	.042402	.013015	.002524	.001257
					.500635
1	998.250000	199.046875	19.228271	9.234863	5.901367
	.499878	.316046	.144031	.055575	.038062
					.016334
m=3					
1	4.505859	2.427734	.859015	.578607	.442169
	.050509	.027340	.008657	.001685	.000839
					.294537
1	26.705078	11.572993	3.193846	2.053711	1.546167
	.242596	.152006	.078432	.031367	.021646
					.009380
2	1406.000000	298.406250	28.937500	13.961914	8.965332
	.850439	.566522	.291608	.137347	.103198
					.055594
m=4					
1	2.316895	1.384009	.559381	.390692	.304724
	.037498	.020852	.006490	.001265	.000631
					.208081
1	7.310059	4.011230	1.512903	1.061755	.840216
	.161060	.105698	.054305	.022016	.015235
					.596948
2	37.839844	16.458496	4.617432	3.004639	2.285645
	.420044	.298444	.165729	.082176	.062512
					.034301
3	1992.750000	397.562500	198.156250	18.679688	12.023926
	1.205054	.822852	.641772	.231244	.181171
					.108234
					2.636475









TABLE I  
PERCENTILES OF THE DISTRIBUTION FUNCTION

$G_m(k; r_1, r_2)$

$r_1 = 1000 \quad r_2 = 500$

K/G

	.001000	.005000	.010000	.050000	.150000	.250000	.500000
	.750000	.850000	.900000	.950000	.990000	.999000	
0	.846686	.569910	.468903	.269421	.157184	.110645	.052626
	.021222	.011882	.007673	.003721	.000362	.000073	
1	1.611279	1.091541	.906219	.546350	.345129	.260297	.149341
	.080768	.056166	.043202	.028474	.008133	.003552	
2	2.981445	1.966980	1.619153	.968109	.619189	.475128	.287946
	.170551	.126788	.102924	.074473	.029516	.016437	
3	6.017822	3.746333	3.013672	1.719922	1.075732	.821356	.501489
	.306189	.233777	.194049	.146228	.067131	.041791	
4	15.301025	8.520508	6.546387	3.377197	1.983459	1.474634	.873419
	.529321	.406158	.339484	.259778	.127856	.084350	
5	70.804668	30.921875	21.468750	8.832031	4.477783	3.113770	1.684155
	.966156	.728680	.604572	.460327	.230389	.156085	
6	3477.125000	693.812500	345.921875	67.583984	21.164063	11.851074	4.779053
	2.272949	1.599988	1.279272	.933441	.441284	.297040	

m=7





TABLE 1  
PERCENTILES OF THE DISTRIBUTION FUNCTION  
 $G_m(k; r_1, r_2)$   
 $r_1 = 1000 \quad r_2 = 500$

K/G

K/G	$r_1 = 1000$		$r_2 = 500$		$G_m(k; r_1, r_2)$	
	.005000 .750000	.010000 .900000	.050000 .950000	.100000 .990000	.150000 .995000	.250000 .999000
0	.691089 .018558	.473785 .010402	.229535 .003260	.168658 .000637	.135394 .000318	.095770 .000063
1	1.237952 .069359	.861914 .048379	.447968 .024614	.344916 .010150	.288037 .007049	.219067 .003080
2	2.099854 .142719	1.443872 .106703	.752545 .063114	.585870 .032725	.494659 .025174	.384619 .014045
3	3.682617 .246716	2.448242 .190173	1.231177 .120410	.953339 .069359	.804266 .055941	.627094 .034968
4	7.199463 .401428	4.500244 .313025	2.091064 .204480	1.586267 .124316	1.323889 .102832	1.020313 .068360
5	17.922363 .654559	9.999268 .508905	3.988770 .334540	2.897705 .208142	2.359131 .174365	1.763806 .119891
6	81.714844 1.149158	35.708984 .873999	24.804688 .729901	10.227051 .561975	5.203613 .292065	3.629639 .203351
7	3070.000000 2.628662	792.187500 1.859436	394.984375 1.492639	37.458984 .640918	24.199219 .531335	13.565918 .364264
						1.979248
						1.059314
						.637317
						.395026
						.237653
						.045850
						.127185
						.237653
						.395026
						.637317
						1.059314
						1.979248
						5.490723

















TABLE I  
PERCENTILES OF THE DISTRIBUTION FUNCTION  $G_m(k; r_1, r_2)$

K/G	$m = 12$				$m = 12$			
	$r_1 = 1000$		$r_2 = 500$		$r_1 = 1000$		$r_2 = 500$	
	.001000 .750000	.005000 .850000	.010000 .900000	.050000 .950000	.100000 .990000	.150000 .995000	.250000 .999000	.500000
0	.394873 .012393	.281995 .006965	.237805 .004506	.144397 .002189	.107776 .000428	.087314 -.000214	.062466 .000043	.030356
1	.626483 .044484	.461792 .031241	.397314 .024160	.259869 .016021	.204907 .006639	.173572 .004617	.134418 .002020	.080124
2	.910309 .086792	.677173 .065647	.586572 .053805	.394415 .039405	.317633 .020654	.273694 .015934	.218518 .008926	.140430
3	1.287756 .139709	.956512 .109695	.829352 .092508	.562677 .071108	.457214 .041730	.397040 .033828	.321539 .021314	.214490
4	1.821655 .206342	1.340247 .165302	1.158557 .141681	.783826 .111957	.638049 .070097	.555536 .058455	.452606 .039401	.307501
5	2.628906 .291486	1.900452 .236218	1.631665 .204388	1.089526 .164203	.883643 .107013	.768384 .0829	.626056 .063874	.428009
6	3.957031 .403717	2.782471 .328925	2.362061 .286023	1.539148 .231976	1.236609 .154855	1.069995 .132983	.867102 .096140	.590509
7	6.414307 .558435	4.323486 .454956	3.605713 .396094	2.257568 .322455	1.783548 .218152	1.529016 .118586	1.224768 .138751	.821906
8	11.857422 .726023	7.471436 .636554	6.056356 .552789	3.554194 .449158	2.731934 .304755	2.303955 .264233	1.807800 .196277	1.178394
9	28.316406 .115665	15.862549 .923401	12.236572 .795667	6.413330 .640796	4.697266 .430878	3.89854 .373206	2.911865 .277631	1.799573
10	125.093750 .1880066	54.742188 .1456140	38.064453 .1233313	15.773193 .972534	10.460449 .636127	8.089600 .57266	5.681396 .403442	3.154297
11	5931.500000 .4045654	1183.750000 .2894531	590.250000 .2344727	115.468750 .1750378	56.089844 .1062793	36.279297 .896216	20.390625 .640033	8.324707

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## APPENDIX

TABLE II

PERCENTILES OF THE DISTRIBUTION FUNCTION

$$G_m(k; r_1, r_2)$$



TABLE II  
PERCENTILES OF THE DISTRIBUTION FUNCTION  $G_m(k; r_1, r_2)$

K/G	m = 1					m = 2					m = 3					m = 4					m = 5																																																																																																																																			
0	.001000 .750000	.005000 .850000	.010000 .500000	.050000 .950000	.100000 .990000	.150000 .995000	.250000 .999000	.500000	0	99.900391 .033332	19.899902 .017646	9.899902 .011112	1.900024 .005264	.900000 .001010	-566675 .000503	-300000 .000100	-100000	0	3.200928 .016891	1.376501 .009271	.544061 .005934	.366522 .002853	.229352 .000554	.168414 .000276	.107074 .000055	.044843	1	197.875000 .101703	39.460939 .064667	19.658691 .047486	3.816650 .029714	1.835571 .011535	1.174670 .007911	.644733 .003403	-242871	2	293.937500 .173663	58.638672 .116840	29.226563 .089893	5.695801 .061119	2.753174 .029214	1.771436 .022039	.983978 .011955	-385779	0	.987122 .011966	.535425 .006545	.403961 .004274	.193073 .002066	.131244 .000403	.100970 -.000201	.067898 .000040	-0.030543	1	5.532227 .053614	2.402832 .036050	1.661023 .027259	.669391 .017658	.433075 .007114	.327612 .004917	.220563 .002135	-1.08752	2	293.937500 .173663	58.638672 .116840	29.226563 .089893	5.695801 .061119	2.753174 .029214	1.771436 .022039	.983978 .011955	-385779	0	.499329 .008529	.300146 .004754	.236005 .003063	.123126 .001483	.086559 .000289	.067803 -.000144	.046582 .000029	-0.021497	1	1.525903 .035361	.840166 .024154	.640552 .018455	.320105 .012046	.225842 .004903	.179401 .003396	.128223 .001479	-0.068413	2	7.677979 .088672	2.343750 .063382	2.216406 .050345	.942932 .035518	.615680 .017746	.469666 .013526	.321417 .007448	-1.66187	3	393.843750 .243604	78.580078 .167407	39.169922 .131152	7.641846 .092218	3.699219 .048123	2.383789 .037837	1.328772 .022744	-527551	0	.364355 .008211	.234479 .004559	.189807 .002971	.105914 .001441	.076628 .000281	.061042 -.000141	.042836 .000028	-0.020345	1	.822089 .031177	.508966 .021646	.407776 .016639	.228497 .010963	.169391 .004510	.138599 .003131	.102924 .001367	-0.058043	2	2.153320 .067604	1.198657 .049825	.520593 .040265	.473511 .029008	.341437 .014900	.276074 .011436	.203595 .006361	-1.17358	3	5.950928 .133472	4.348145 .099168	3.019775 .081146	1.243933 .060162	.820410 .033687	.631213 .026983	.438812 .016693	-2.36249	4	480.500000 .317084	95.886719 .222943	47.808594 .177814	9.345947 .128833	4.536133 .072008	2.931152 .058302	1.643689 1.643689	-665210





TABLE II

PERCENTILES OF THE DISTRIBUTION FUNCTION

 $G_m(k; r_1, r_2)$  $r_1 = 100$  $r_2 = 10$ 

K/G

K/G	.001000 .750000	.005000 .850000	.010000 .900000	.050000 .950000	.100000 .990000	.150000 .995000	.250000 .999000	.500000
0	.198627 .006168	.139758 .003471	.117358 .002246	.070978 .001092	.053031 -.000214	.043015 .000106	.030845 .000021	.015056
1	.330939 .071814	.235659 .015346	.200269 .011879	.128192 .007889	.100482 .003274	.084915 .002277	.065667 .000997	.039176
2	.526086 .042233	.368658 .031962	.312018 .026208	.200299 .019214	.158710 .010089	.135638 .007785	.107349 .004368	.068451
3	.867590 .068363	.585626 .053488	.488556 .045056	.305334 .034606	.240399 .020314	.205182 .016471	.162891 .010387	.106097
4	1.598657 .103625	1.010425 .082226	.820380 .070143	.483490 .055152	.372198 .034362	.314001 .028634	.246136 .019283	.159015
5	3.758301 .156512	2.111084 .124042	1.631360 .106036	.860144 .084057	.632281 .053904	.519525 .045590	.394293 .031894	.244550
6	16.218018 .252515	7.106689 .195911	4.946533 .165851	2.058838 .130298	1.370276 .083576	1.062671 .071039	.749890 .050582	.420380
7	747.250000 .524652	149.140625 .378088	74.380859 .307684	14.565430 .230969	7.085205 .140643	4.589355 .118335	2.587402 .083488	1.065906
0	.230420 .006651	.158832 .003738	.132251 .002418	.078520 .001175	.058241 -.000230	.047047 .000115	.033572 .000023	.016288
1	.408478 .023881	.282170 .016754	.236737 .012950	.147205 .008585	.114001 .003556	.095667 .002473	.073336 .001082	.043225
2	.709271 .047292	.475189 .035558	.394568 .029107	.242444 .021264	.188556 .011116	.159381 .008571	.124377 .004798	.077711
3	1.348059 .079207	.848639 .061402	.687274 .051455	.401154 .039271	.306616 .022855	.27184 .018485	.199603 .011619	.125781
4	3.235840 .126971	1.814209 .099134	1.400049 .083793	.734265 .065140	.537561 .039958	.440186 .033156	.332037 .022176	.202802
5	14.171143 .213300	6.205566 .163867	4.317139 .137683	1.792676 .106769	1.190662 .066441	.921722 .055735	.648212 .038478	.360083
6	660.000000 .456635	131.734375 .327124	65.691406 .264935	12.858398 .197223	6.251465 .117664	4.047119 .098104	2.278809 .067723	.934814

m=7



TABLE II

## PERCENTILES OF THE DISTRIBUTION FUNCTION

 $G_m(k; r_1, r_2)$  $K/G$  $r_1 = 100$  $r_2 = 10$ 

	.001000	.005000	.010000	.050000	.100000	.150000	.250000	.500000
	.750000	.850000	.900000	.950000	.990000	.995000	.999000	

m=8

0	.279736	.127457	.154285	.089306	.065575	.052672	.037334	.017955
	.007237	.004056	.002648	.001285	.000251	-.000125	.000025	
1	.544767	.359747	.296368	.176837	.134601	.111835	.084648	.049031
	.024783	.018714	.014434	.009546	.003943	.002741	.001199	
2	1.090198	.682086	.550226	.316443	.239240	.198971	.151935	.092092
	.054892	.040950	.033366	.024447	.012592	.009691	.005413	
3	2.701416	1.510409	1.163379	.605548	.440704	.359106	.268536	.160358
	.097265	.074289	.061734	.046635	.026773	.021581	.013484	
4	12.083005	7.286621	5.675293	1.521143	1.007434	.777236	.544550	.298688
	.173612	.131580	.109363	.083294	.049695	.040325	.027051	
5	71.125699	43.94375	30.835938	11.118896	5.401855	3.494385	1.964233	.811245
	.276603	.216631	.163135	.094717		.078013	.052313	

m=9

0	.176624	.126239	.106708	.065422	.049149	.039985	.028775	.014114
	.006756	.003263	.002112	.001027	-.000201	.000100	.000020	
1	.281567	.205050	.175952	.115039	.090974	.072269	.060135	.036193
	.020264	.014288	.011074	.007362	.003059	.002129	.000932	
2	.621967	.305243	.261853	.172389	.135240	.119422	.095869	.062001
	.038623	.029340	.024110	.017719	.009334	.007211	.004048	
3	.638049	.450089	.303673	.250958	.201520	.174330	.140247	.093393
	.061127	.043123	.040621	.031383	.018528	.015345	.009510	
4	1.020923	.692004	.573553	.366278	.290723	.249738	.200452	.134082
	.089580	.071761	.061556	.048779	.030696	.025647	.017345	
5	1.843075	1.168722	.900256	.563867	.436279	.369512	.291730	.191760
	.127979	.103183	.080073	.071467	.046616	.039815	.027929	
6	4.269531	2.40155	1.857840	.993368	.725079	.597752	.455322	.285596
	.185748	.149752	.128314	.103137	.068283	.058550	.042290	
7	15.225342	7.990244	5.563321	2.315824	1.546411	1.200964	.840646	.479645
	.291180	.227582	.193774	.153735	.100909	.086616	.063118	
8	12.2937500	166.250000	82.510156	16.240723	7.903564	5.121582	2.890381	1.146690
	.601516	.428223	.349768	.264294	.163562	.138595	.094435	



TABLE II

PERCENTILES OF THE DISTRIBUTION FUNCTION

 $G_m(k; r_1, r_2)$  $r_1 = 100 \quad r_2 = 10$ 

K/G

	.005000	.010000	.050000	.100000	.150000	.250000	.500000
0	.005000	.010000	.050000	.100000	.150000	.250000	.500000
1	.005000	.010000	.050000	.100000	.150000	.250000	.500000
2	.005000	.010000	.050000	.100000	.150000	.250000	.500000
3	.005000	.010000	.050000	.100000	.150000	.250000	.500000
4	.005000	.010000	.050000	.100000	.150000	.250000	.500000
5	.005000	.010000	.050000	.100000	.150000	.250000	.500000
6	.005000	.010000	.050000	.100000	.150000	.250000	.500000
7	.005000	.010000	.050000	.100000	.150000	.250000	.500000
8	.005000	.010000	.050000	.100000	.150000	.250000	.500000
9	.005000	.010000	.050000	.100000	.150000	.250000	.500000

m=10

	.061169	.066143	.07623	.087604	.108783	.124988	.141639	.157999	.172290	.184854	.194545	.201362
0	.061169	.066143	.07623	.087604	.108783	.124988	.141639	.157999	.172290	.184854	.194545	.201362
1	.066143	.07623	.087604	.108783	.124988	.141639	.157999	.172290	.184854	.194545	.201362	.208154
2	.07623	.087604	.108783	.124988	.141639	.157999	.172290	.184854	.194545	.201362	.208154	.214946
3	.087604	.108783	.124988	.141639	.157999	.172290	.184854	.194545	.201362	.208154	.214946	.221738
4	.108783	.124988	.141639	.157999	.172290	.184854	.194545	.201362	.208154	.214946	.221738	.228530
5	.124988	.141639	.157999	.172290	.184854	.194545	.201362	.208154	.214946	.221738	.228530	.235322
6	.141639	.157999	.172290	.184854	.194545	.201362	.208154	.214946	.221738	.228530	.235322	.242114
7	.157999	.172290	.184854	.194545	.201362	.208154	.214946	.221738	.228530	.235322	.242114	.248906
8	.172290	.184854	.194545	.201362	.208154	.214946	.221738	.228530	.235322	.242114	.248906	.255698
9	.184854	.194545	.201362	.208154	.214946	.221738	.228530	.235322	.242114	.248906	.255698	.262490





TABLE II

## PERCENTILES OF THE DISTRIBUTION FUNCTION

 $G_m(k; r_1, r_2)$ 

K/G	$r_1 = 200$			$r_2 = 20$		
	.005000 .001000 .000000	.010000 .005000 .000000	.050000 .025000 .000000	.900000 .950000 1.000000	.990000 .995000 1.000000	.999000 1.000000 1.000000
$m = 1$						
0	53.900391 .033332	19.899902 .017646	9.899902 .011112	1.900024 .005264	.900000 .001010	.300000 .000100
0	1.132813 .016115	1.345862 .008869	.522363 .005672	.357001 .007725	.222882 .000529	.103595 .000053
1	198.859375 .100848	39.654297 .063950	19.753906 .046876	3.832764 .029264	1.842102 .011325	.645557 .003335
$m = 2$						
0	.944458 .011016	.510614 .006107	.384436 .003924	.182422 .001895	.123462 -.000369	.063366 .000037
1	5.440186 .051058	2.360107 .034236	1.630078 .025834	.654437 .016662	.422115 .006689	.213605 .002005
2	296.843750 .171985	59.212941 .115141	29.509766 .082883	5.746826 .059748	2.775146 .028352	.988739 .011539
$m = 3$						
0	.534540 .009509	.323157 .005359	.254926 .003457	.134387 .001675	.095045 .000327	.051646 .000032
1	1.580755 .038524	.876532 .026450	.649666 .020253	.337164 .013259	.239056 .005417	.137012 .001637
2	7.770712 .093271	3.388428 .067044	2.349365 .053450	.960413 .037887	.629199 .019062	.330908 .008039
3	388.125000 .245740	77.443459 .169371	38.607422 .133746	7.538574 .044648	3.653320 .045924	1.316992 .023809
$m = 5$						
0	.332129 .007068	.212079 .003952	.170917 .002550	.094179 .001236	.067677 -.000241	.037440 .000024
1	.772443 .027625	.475615 .019107	.379858 .014652	.210645 .009626	.155170 .003946	.093229 .001195
2	2.080811 .061943	1.154529 .045384	.884802 .036548	.451599 .026208	.323920 .013370	.191180 .005684
3	5.879180 .126941	4.311035 .093656	2.991211 .076288	1.226721 .056201	.806159 .031158	.427765 .015319
4	489.906250 .315039	97.755859 .219861	48.726328 .174457	9.518555 .125415	4.614258 .069134	1.665601 .035583



TABLE II  
PERCENTILES OF THE DISTRIBUTION FUNCTION  
 $r_1 = 200 \quad r_2 = 20$   
 $G_m(k; r_1, r_2)$

K/C	$r_1 = 200$	$r_2 = 20$	$G_m(k; r_1, r_2)$
	m=6		
0	.001000 .750000	.005000 .850000	.000000 .500000
1	.248883 .006105	.165210 .003422	.045010 .000021
2	.499146 .023031	.327765 .016025	.098978 .001016
3	1.029651 .049650	.640765 .036117	.182208 .004682
4	2.623047 .089168	1.461633 .067627	.340765 .011947
5	12.052246 .165383	5.276113 .124316	.765424 .037551
6	85.062500 .386053	116.750000 .272168	3.566406 .074347
	m=7		
0	.200269 .005424	.136554 .003044	.039161 .000093
1	.366370 .019973	.250836 .013958	.082363 .002043
2	.654681 .040673	.435486 .030442	.141823 .007223
3	1.279456 .070265	.801184 .054055	.236676 .015949
4	3.156434 .116595	1.763806 .090252	.419434 .029378
5	14.200684 .203656	6.210205 .155073	.910797 .034892
6	79.250000 .456512	135.546875 .324154	2.329590 .063683



TABLE II  
PERCENTILES OF THE DISTRIBUTION FUNCTION

K/G	r <sub>1</sub> = 200		r <sub>2</sub> = 20		G <sub>m</sub> (k; r <sub>1</sub> , r <sub>2</sub> )	
	r <sub>1</sub> = 200	r <sub>2</sub> = 20	r <sub>1</sub> = 200	r <sub>2</sub> = 20	G <sub>m</sub> (k; r <sub>1</sub> , r <sub>2</sub> )	
m = 8						
0	.001000 .750000	.005000 .850000	.010000 .500000	.050000 .950000	.150000 .995000	.500000
1	.168711 .004916	.117389 .002762	.058379 .000867	.043298 -.000170	.034957 .000084	.012062
2	.290204 .017791	.204602 .012470	.109027 .006384	.084770 .002642	.071257 .001837	.032245
3	.474792 .035354	.323840 .026613	.175830 .015888	.138202 .008299	.117480 .006395	.057986
4	.805029 .058878	.539545 .045758	.276624 .029329	.216107 .017074	.183490 .013813	.092661
5	1.524561 .092096	.958527 .072493	.452301 .040055	.345801 .029622	.290234 .024602	.143542
6	3.682861 .144010	2.062012 .113116	.831519 .075594	.607745 .047826	.497162 .040276	.228772
7	16.326172 .241742	7.144287 .185748	2.057861 .121600	1.364294 .076708	1.054614 .064846	.409180
8	772.500000 .526392	154.171875 .375820	15.039307 .225629	7.306396 .134692	4.726074 .112537	1.084644
m = 9						
0	.146930 .004523	.103748 .002543	.052630 .000799	.039249 -.000156	.031791 .000078	.011066
1	.241650 .016162	.174060 .011352	.095552 .005825	.074957 .002416	.063332 .001679	.029111
2	.372595 .031547	.266858 .023843	.148486 .014305	.118243 .007499	.101276 .005785	.051222
3	.579095 .051257	.405752 .040097	.221537 .025914	.176440 .015186	.151508 .012306	.079390
4	.951936 .077249	.661315 .061452	.333502 .041314	.262616 .025739	.224347 .021440	.117511
5	1.765881 .113971	1.113452 .091077	.529932 .062268	.407135 .040112	.343054 .033954	.173663
6	4.203125 .171344	2.356689 .135174	.954895 .092798	.699969 .060513	.573969 .051631	.268109
7	17.429666 .216321	8.068604 .216321	2.329102 .183665	1.546411 .092573	1.197009 .078981	.468628
8	366.337500 .595697	172.609375 .427063	16.844238 .258801	8.186523 .156757	5.297607 .131324	1.220740











TABLE II

PERCENTILES OF THE DISTRIBUTION FUNCTION  $G_m(k; r_1, r_2)$ 

K/C	r <sub>1</sub> = 300		r <sub>2</sub> = 30		G <sub>m</sub> (k; r <sub>1</sub> , r <sub>2</sub> )
	r <sub>1</sub> = 300		r <sub>2</sub> = 30		
	.001000	.005000	.010000	.050000	.150000
	.750000	.650000	.500000	.990000	.999000
					.500000
0	99.900391	19.899902	9.899902	1.900024	.900000
	.033332	.017666	.011112	.005264	.000100
					.100000
0	3.109375	1.335425	.914978	.353766	.161670
	.015945	.008735	.005584	.002684	.000259
1	199.187500	39.718750	19.785645	3.838379	1.844299
	.100574	.063706	.046570	.029111	.011257
					.645831
					.003312
0	.929871	.502130	.377783	.178821	.092531
	.010700	.005926	.003608	.001839	.000178
					.042573
1	5.408447	2.345459	1.619458	.649310	.315466
	.050192	.033610	.025342	.016330	.004520
2	297.812500	59.408203	29.605469	5.764160	1.787976
	.111405	.114551	.087734	.059279	.021108
					.990356
					.011398
0	.487213	.292249	.229504	.119281	.065452
	.006173	.004552	.002931	.001419	.000138
					.020643
1	1.504846	.827612	.630511	.314246	.175586
	.034282	.023470	.017849	.011638	.003276
2	7.645752	3.328369	2.304688	.936890	.465668
	.087108	.062134	.049294	.034713	.013179
3	195.796875	78.964844	39.361328	7.677002	2.393066
	.242871	.166553	.130267	.091390	.037307
					1.332800
					.022378
0	.321021	.204358	.164447	.090185	.051184
	.006657	.003736	.002410	.001168	.000114
					.016704
1	.755400	.444081	.370184	.204480	.122211
	.026441	.018253	.013984	.009178	.002606
2	2.055420	1.139148	.872351	.444000	.255658
	.060017	.043881	.035289	.025262	.009844
3	9.853516	4.298096	2.580957	1.220679	.801215
	.124713	.091779	.074633	.054854	.030299
4	493.125000	98.394531	49.052724	9.577637	2.994141
	.314368	.218823	.173257	.124255	.054846
					1.673169
					.034915



TABLE II  
PERCENTILES OF THE DISTRIBUTION FUNCTION

$r_1 = 300$   $r_2 = 30$   $G_m(k; r_1, r_2)$

K/G

K/G	$r_1 = 300$ $r_2 = 30$		$G_m(k; r_1, r_2)$	
	$r_1 = 300$	$r_2 = 30$	$G_m(k; r_1, r_2)$	$G_m(k; r_1, r_2)$
<b>m = 6</b>				
0	.001060 .750000	.005000 .850000	.010000 .500000	.150000 .995000
1	.238232 .005718	.157556 .003197	.128772 .002044	.042420 .000097
2	.483582 .021764	.316656 .015121	.259412 .011627	.094591 .002187
3	1.008411 .046529	.626331 .034469	.503076 .027925	.176471 .007972
4	2.595215 .086407	1.444482 .065354	1.103424 .053977	.334387 .018402
5	12.040283 .162524	5.258545 .121844	3.650635 .100543	.761060 .036399
6	589.812500 .385596	117.703125 .271100	58.681641 .216443	3.591309 .073084
<b>m = 7</b>				
0	.189807 .005014	.128894 .002812	.106525 .001818	.036502 .000086
1	.351660 .018667	.239441 .013015	.199969 .010032	.077822 .001895
2	.635516 .038428	.421600 .028703	.348120 .023362	.135760 .006769
3	1.255266 .067211	.784497 .051609	.632556 .042989	.229565 .015087
4	3.128174 .113025	1.745923 .087261	1.363620 .073229	.42201 .026089
5	14.208984 .200330	6.210938 .152057	4.314941 .126697	.906921 .049344
6	685.875000 .456512	136.875000 .323187	68.246094 .259503	4.184570 .091711









TABLE II  
PERCENTILES OF THE DISTRIBUTION FUNCTION  $G_m(k; r_1, r_2)$

K/G	$r_1 = 300$		$r_2 = 30$		$G_m(k; r_1, r_2)$	
	.001000 .750000	.005000 .850000	.050000 .950000	.100000 .900000	.150000 .995000	.250000 .999000
0	.120685 .003779	.085792 .002126	.043824 .000668	.032729 -.000131	.026525 .000065	.018993 -.000013
1	.194537 .013492	.141772 .009461	.078917 .004866	.062115 .002018	.052577 .001404	.040704 .000614
2	.290906 .026246	.212201 .019855	.120868 .011928	.096838 .006256	.083225 .004826	.066262 .002705
3	.431274 .042332	.310706 .033187	.175952 .021501	.141589 .012622	.122302 .010231	.098425 .006449
4	.657306 .062985	.461923 .050307	.254315 .033577	.203595 .021241	.175616 .017711	.141437 .011936
5	1.069934 .090627	.721478 .072985	.376593 .050376	.297314 .032680	.254559 .027711	.203412 .019458
6	1.975708 .130145	1.246009 .104785	.593683 .072821	.456573 .048135	.385077 .041219	.302069 .029683
7	4.697510 .192920	2.633545 .153674	1.067004 .105914	.782300 .070177	.641589 .060330	.485748 .044003
8	20.621094 .312933	9.027344 .242474	2.604980 .161761	1.729199 .105182	1.338232 .090150	.941071 .065728
9	970.375000 .666949	193.656250 .478088	18.895264 .285929	9.182129 .176196	5.941162 .148486	3.342041 .105640







TABLE II  
PERCENTILES OF THE DISTRIBUTION FUNCTION

K/G	$r_1 = 400$		$r_2 = 40$		$G_m(k; r_1, r_2)$	
	$r_1 = 400$	$r_2 = 40$	$r_1 = 400$	$r_2 = 40$	$r_1 = 400$	$r_2 = 40$
<b>m=6</b>						
0	.001000 .750000	.005000 .850000	.010000 .500000	.050000 .950000	.150000 .995000	.250000 .999000
1	.232800 .005508	.153674 .003084	.125507 .001991	.071043 .000965	.041119 .000094	.028859 .000019
2	.475647 .021131	.311011 .014667	.254559 .011272	.148914 .007421	.092374 .002117	.069138 .000924
3	.997620 .045461	.619006 .034641	.496857 .027234	.281079 .019649	.173541 .007755	.131091 .004313
4	2.581055 .085010	1.435754 .064209	1.102283 .052985	.566766 .039641	.331152 .017997	.245068 .011165
5	12.033936 .161090	5.254355 .120593	3.647217 .099409	1.499170 .074816	.987274 .043759	.526788 .023420
6	592.250000 .385362	118.171875 .270551	58.519922 .215771	11.510498 .156665	5.581787 .088711	2.017334 .047822
<b>m=7</b>						
0	.184528 .004810	.125018 .002697	.103158 .001742	.058832 .000846	.035167 .000083	.024850 .000016
1	.344153 .017997	.234387 .012546	.195148 .009664	.118640 .006380	.075529 .001827	.057219 .000798
2	.625751 .037299	.414520 .027829	.341986 .022634	.205975 .016422	.132709 .006540	.102283 .003648
3	1.242896 .065674	.775952 .050353	.625293 .041905	.358923 .031688	.225934 .014652	.173236 .009146
4	3.113525 .111224	1.736768 .085731	1.335852 .071871	.691974 .055235	.409508 .027440	.304816 .018173
5	14.211897 .198627	6.211182 .150531	4.314453 .125293	1.778882 .095846	.904907 .048516	.630969 .033042
6	189.250000 .456543	137.546875 .322699	68.578125 .258832	13.404297 .189777	4.202393 .090883	2.356201 .061585





TABLE II  
PERCENTILES OF THE DISTRIBUTION FUNCTION  
 $r_1 = 400$   $r_2 = 40$

K/G

		$r_1 = 400$	$r_2 = 40$	$G_m (k, r_1, r_2)$	
0	.001000 .750000	.005000 .850000	.050000 .950000	.150000 .995000	.500000
1	.153217 .004290	.105823 .002407	.051951 .000755	.030879 .000074	.010559
2	.268719 .015762	.188281 .011024	.099096 .005625	.064251 .001615	.028730
3	.447510 .031828	.302271 .023898	.163043 .014202	.108051 .005691	.052626
4	.771527 .054011	.515009 .041802	.261487 .026632	.172107 .012462	.085720
5	1.484644 .086128	.930634 .067478	.435699 .044408	.277692 .015041	.135486
6	3.641602 .137500	2.035156 .107471	.816138 .071222	.485260 .037540	.220502
7	16.379395 .236127	7.162558 .180459	2.056885 .117084	1.050220 .061638	.403290
8	78.812590 .527429	15.612500 .374731	15.288574 .222513	4.798096 .109546	1.094592
9	131427 .003886	.092104 .002183	.046109 .000685	.027646 .000067	.009538
10	.220563 .014087	.157794 .009874	.085487 .005054	.056189 .001454	.025522
11	.346257 .027928	.246533 .021055	.135486 .012577	.091619 .005064	.045708
12	.547348 .046193	.381659 .035991	.206036 .023126	.139728 .010913	.072161
13	.914764 .070955	.613727 .056174	.316077 .037478	.210950 .019290	.108875
14	1.723828 .106677	1.083728 .084820	.877142 .072584	.328986 .031039	.164203
15	4.166016 .163806	2.331543 .129260	.939423 .087437	.561517 .048051	.258893
16	18.523691 .273511	8.108399 .210461	2.333496 .138416	1.194690 .075018	.462799
17	881.875000 .598016	175.984375 .426575	17.163818 .255994	5.390869 .128314	1.234595









TABLE II

PERCENTILES OF THE DISTRIBUTION FUNCTION

 $G_m(k; r_1, r_2)$ 

K/G

 $r_1 = 500$  $r_2 = 50$ 

K/G	$r_1 = 500$		$r_2 = 50$		$G_m(k; r_1, r_2)$	
	$r_1 = 500$	$r_2 = 50$	$r_1 = 500$	$r_2 = 50$	$G_m(k; r_1, r_2)$	$G_m(k; r_1, r_2)$
0	.001000	.005000	.010000	.050000	.150000	.250000
	.750000	.850000	.900000	.950000	.990000	.999000
$m = 1$						
0	95.900391	19.859902	1.900024	.900000	.566575	.300000
	.033332	.017645	.005264	.001010	.000503	.000100
$m = 2$						
0	3.096870	1.327002	.351172	.218915	.160297	.101428
	.015755	.005621	.002649	.000514	.000256	.000051
1	199.453175	39.771484	4.842773	1.846008	1.179780	.646075
	.100560	.063511	.028589	.011199	.007671	.003294
$m = 3$						
0	.918030	.495270	.175891	.118671	.090810	.060604
	.010448	.005713	.001793	.000349	.000174	.000035
1	5.382813	2.333496	.645129	.415344	.312964	.209332
	.049496	.033107	.016059	.006431	.004440	.001924
2	298.609375	59.564453	5.777032	2.786574	1.791333	.991638
	.170927	.114093	.058901	.027822	.020917	.011283
$m = 4$						
0	.477376	.285840	.116199	.081352	.063553	.043496
	.007877	.004350	.001367	.000267	.000133	.000026
1	1.487744	.817419	.309485	.217633	.172472	.122821
	.033410	.022758	.011310	.004592	.003175	.001384
2	7.617325	3.315674	.931976	.607227	.462402	.315497
	.085846	.061131	.034064	.016541	.012897	.007086
3	497.375060	79.277344	7.705322	3.727539	2.400391	1.336096
	.242231	.165241	.090723	.047005	.036880	.022081
$m = 5$						
0	.311957	.198108	.086956	.062195	.049180	.034160
	.006372	.003564	.001113	.000217	.000108	.000022
1	.741132	.454651	.199512	.146350	.118823	.087261
	.025440	.017566	.008819	.003607	.002500	.001090
2	2.034666	1.126575	.437836	.312964	.251416	.183490
	.058466	.042664	.024499	.012439	.009519	.005270
3	9.832275	4.287109	1.215796	.797132	.610431	.420837
	.122913	.090257	.053763	.029603	.023591	.014473
4	495.734375	98.912109	9.625244	4.662842	3.007080	1.679211
	.313818	.217969	.123309	.067356	.054125	.034373



TABLE II  
PERCENTILES OF THE DISTRIBUTION FUNCTION

K/G	r <sub>1</sub> = 500			r <sub>2</sub> = 50			G <sub>m</sub> (k; r <sub>1</sub> , r <sub>2</sub> )		
	.001000	.005000	.010000	.050000	.100000	.150000	.250000	.500000	
	.750000	.850000	.900000	.950000	.990000	.995000	.999000		
m=6									
0	.229535	.151324	.123452	.069794	.050616	.040337	.028287	.013397	
	.004390	.003016	.001947	.000944	-.000184	.000092	.000018		
1	.470556	.307593	.251660	.146960	.110492	.091035	.068074	.038615	
	.020746	.014392	.011058	.007278	.002991	.002075	.000906		
2	.901089	.614551	.493103	.278607	.208295	.171802	.129657	.076796	
	.044820	.033141	.026819	.019340	.009533	.007623	.004239		
3	2.572510	1.430644	1.057949	.564050	.406769	.329155	.243420	.142078	
	.084167	.063519	.052386	.039165	.022126	.017753	.011009		
4	12.025785	5.251953	3.645264	1.497583	.985840	.757458	.525568	.252422	
	.160236	.119430	.090726	.074232	.043355	.035464	.023168		
5	92.687500	118.468750	59.064452	11.537538	5.594238	3.61328	2.020996	.813361	
	.389260	.270215	.215375	.156207	.088295	.072065	.047509		
m=7									
0	.181323	.122660	.101184	.058558	.042882	.034362	.024263	.011592	
	.004667	.002627	.001657	.000824	-.000161	.000080	.000016		
1	.335636	.231030	.192249	.116656	.089145	.074144	.056117	.032386	
	.017601	.012264	.009443	.006231	.002568	.001783	.000779		
2	.619800	.410217	.339293	.203412	.156177	.10847	.100757	.061467	
	.036620	.027259	.021155	.016094	.008329	.006405	.003570		
3	1.235227	.770764	.620558	.355963	.268994	.223767	.171405	.105334	
	.064743	.049556	.041253	.031169	.017868	.014392	.008978		
4	3.104736	1.731213	1.31213	.684953	.459695	.406281	.302924	.180530	
	.110126	.084308	.071951	.054553	.032802	.027047	.017898		
5	14.215332	6.211426	4.213965	1.772844	1.173450	.903717	.629749	.342352	
	.197620	.140585	.124438	.095094	.057711	.048020	.032664		
6	691.312500	137.953125	68.781250	13.642383	6.522217	4.213379	2.361572	.955231	
	.456543	.322476	.258405	.159258	.105946	.090383	.061158		





TABLE II

## PERCENTILES OF THE DISTRIBUTION FUNCTION

 $G_m(k; r_1, r_2)$  $r_1 = 500 \quad r_2 = 50$ 

K/G

K/G	$r_1 = 500 \quad r_2 = 50$		$G_m(k; r_1, r_2)$	
	0.01000	0.05000	0.50000	0.99000
0	.001000 .750000	.005000 .150000	.010000 .500000	.100000 .990000
1	.001004 .004164	.003473 .002326	.006017 .001510	.037356 -.000143
2	.004325 .015364	.014455 .010730	.015715 .008278	.075045 .002260
3	.004185 .031142	.005060 .023347	.005414 .013862	.125354 .007210
4	.004630 .053023	.009943 .041005	.022516 .034299	.200757 .015094
5	.004734 .034713	.009456 .066464	.032312 .043671	.328955 .026700
6	.003307 .136103	.002715 .106311	.012964 .070337	.591943 .044057
7	.003498 .163498	.001601 .179431	.005664 .116168	1.360144 .072428
8	.000000 .527623	.003275 .374518	.003360 .222363	7.446533 .131000
m=9				
0	.128284 .003759	.009741 .002110	.044797 .000663	.033221 -.000130
1	.016286 .013671	.014468 .009578	.083446 .004892	.065056 .002026
2	.040857 .037233	.023352 .020494	.132831 .012229	.105121 .006384
3	.040857 .045171	.036685 .035163	.202863 .022565	.160602 .013141
4	.007074 .069668	.068051 .055058	.312476 .036704	.244702 .022691
5	.171510 .105212	.107752 .083546	.057959 .056552	.388373 .036082
6	.415823 .162230	.232646 .127917	.936218 .086348	.683673 .055670
7	.185546 .272290	.116455 .209271	.233422 .137347	1.546045 .087368
8	.085312 .598474	.087500 .426483	17.229248 .255444	8.366943 .152545
			5.410156 .127612	3.038574 .089294



TABLE II  
PERCENTILES OF THE DISTRIBUTION FUNCTION  $G_m(k, r_1, r_2)$

K/G	$r_1 = 500$				$r_2 = 50$				$G_m(k, r_1, r_2)$	
	.001000	.005000	.010000	.050000	.100000	.500000	.900000	.950000		
0	.001000	.005000	.010000	.050000	.100000	.500000	.900000	.950000	.150000	.500000
1	.001000	.005000	.010000	.050000	.100000	.500000	.900000	.950000	.150000	.500000
2	.001000	.005000	.010000	.050000	.100000	.500000	.900000	.950000	.150000	.500000
3	.001000	.005000	.010000	.050000	.100000	.500000	.900000	.950000	.150000	.500000
4	.001000	.005000	.010000	.050000	.100000	.500000	.900000	.950000	.150000	.500000
5	.001000	.005000	.010000	.050000	.100000	.500000	.900000	.950000	.150000	.500000
6	.001000	.005000	.010000	.050000	.100000	.500000	.900000	.950000	.150000	.500000
7	.001000	.005000	.010000	.050000	.100000	.500000	.900000	.950000	.150000	.500000
8	.001000	.005000	.010000	.050000	.100000	.500000	.900000	.950000	.150000	.500000
9	.001000	.005000	.010000	.050000	.100000	.500000	.900000	.950000	.150000	.500000



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ABSTRACT

As in the Polaris A3 program, whenever extensive test data collected under non-environmental conditions must be used to infer results valid under environmental conditions, the problem of estimation of a correction factor to transform non-environmental results into environmental ones will arise. In the Polaris A3 program, the ratio of mean times under environmental and non-environmental conditions was termed the K-factor. This report presents a solution to the problem of building exact confidence intervals for the K-factor for the case when time is measured in cycles. This was the remaining open question in the problem of point and interval estimation of the K-factor.





K-factor Estimation

Statistical Estimation

Confidence Intervals

Ratio of Bernoulli Parameters



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